**Dimensional analysis** is the technique of treating units as numbers for the purpose of solving problems. For mathematical purposes 1 ft means  $1 \times \text{ft}$ . (Numbers are multiplied by their units.) Write a ratio with one unit on bottom and another unit on the top. Insert numbers to make the top and bottom *equal* to use as a conversion factor.

- Words that mean divided: per, in a, is a, are a, goes with, equals, equivalent
- Recognize that there is a difference between \$/lb and lb/\$.
- Metric prefixes can be treated as independent units:  $\frac{\text{milli}}{0.001} \frac{\text{kilo}}{1000} \frac{\text{centi}}{0.01}$
- Converting 6 m<sup>2</sup> to square ft requires using a conversion twice.  $\sec \times \sec = \sec^2 \qquad \qquad 3^2 \times 3^2 = 3^4$  $m^2 \times m = m^3$
- Always identify amount of what or moles of what. Having 2 mL or 4 grams or 3 mole is less meaningful than having 2 mL H<sub>2</sub>O or 4 grams He or 3 mole C.

## Most numerical chemistry problems involve

## 1. converting from amounts to moles

Grams of solid converted to moles using formula mass: FM g/mole.

Liters of liquid converted to grams using density in g/mL, then grams converted to moles using formula mass. The density of liquid water from 0 to 30°C is 1.00 g/mL.

Liters of solution converted to moles using molarity. Grams of solution converted to

grams dissolved using %, then grams converted to moles using formula mass.

Molarity = 
$$\frac{\text{moles dissolved}}{\text{liters of solution}} = M$$
 % =  $\frac{\text{g dissolved}}{100 \text{ g solution}}$  ppm =  $\frac{\text{mg analyte}}{\text{kg sample}}$  or  $\frac{\text{mg analyte}}{\text{L solution}}$ 

The number of moles or grams dissolved does not change upon dilution.

Liters of gas converted to moles using 
$$\frac{PV}{nT} = \frac{.082058 \text{ L atm}}{\text{mol K}}$$
.

2. **using stoichiometry information from formulas or balanced reactions**

$$CO_{2} \text{ means } \frac{2 \text{ atoms O}}{1 \text{ atom C}} \text{ or } \frac{2 \text{ atoms O}}{\text{molecule CO}_{2}} \text{ or } \frac{1 \text{ atom C}}{2 \text{ atoms O}}, \text{ etc.}$$

$$2H_{2} + O_{2} \rightarrow 2H_{2}O \text{ means } \frac{2 \text{ molecules H}_{2}}{1 \text{ molecule O}_{2}} \text{ or } \frac{2 \text{ molecules H}_{2}O}{1 \text{ molecule O}_{2}}, \text{ etc.}$$

3. converting from moles to amounts

Example: How many g Ag in 3.72 g Ag<sub>2</sub>CO<sub>3</sub>?

$$3.72 \text{ g Ag}_2\text{CO}_3 \quad \frac{\text{mol Ag}_2\text{CO}_3}{275.8 \text{ g Ag}_2\text{CO}_3} \frac{2 \text{ mol Ag}}{\text{mol Ag}_2\text{CO}_3} \frac{107.9 \text{ g Ag}}{\text{mol Ag}} = 2.91 \text{ g Ag}$$

Example: 10.02 mL HCl is titrated with 0.1123 mol NaOH/L. The indicator changes color after addition of 42.34 mL NaOH. What is the mol HCl/L?

- a. Convert amount delivered from buret to moles
- b. Use stoichiometry of reaction: 1 HCl + 1 NaOH  $\rightarrow$  1 NaCl + 1 H<sub>2</sub>O
- c. Moles/L wanted so take moles and divide by original liters.

$$\frac{42.34 \text{ mL NaOH}}{\frac{\text{L NaOH}}{10.02 \text{ mL HCl}}} \frac{1 \text{mol HCl}}{1 \text{mol NaOH}} = 0.4745 \text{ mol HCl/L}$$

## Symbols for molarity = mol/L

In analytical chemistry we need to make a distinction between how a solution is prepared and the species that are actually in the solution. We will use M for the "analytical concentration" (the total amount, or the recipe), and [] for the actual solution species concentration. Both are read as mol/L.

For example, in 1.0 M NaCl, the [NaCl] = 0.0,  $[Na^+]$  = 1.0, and  $[Cl^-]$  = 1.0, and in  $1.00 \text{ M H}_2\text{SO}_4$ ,  $[\text{H}_2\text{SO}_4] = 0.000$ ,  $[\text{HSO}_4] = 0.988$ ,  $[\text{SO}_4] = 0.012$ , and  $[\text{H}^+] = 1.012$ 

